

# Analysis of Trim and Compressibility Effects in Extended Formation Flight



Mr. James Kless, Mr. Michael J. Aftosmis, and Dr. Marian Nemec

Aerospace Engineer  
NASA Ames Research Center

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Subsonic Fixed Wing Project  
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## Overview



- Extended formation flight
- Modeling approach
- Results
  - Mesh convergence study
  - Incompressible effects
    - Vortex position sensitivity
    - roll-trim
  - Compressible effects
    - roll-trim
- Summary
  - Current efforts



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## Background: Close Formations



14% reduction in heart rate when in formation (Welmerskirch, et. al, 2001)

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## Background: Close Formations



Over 20% drag reduction and 18% fuel flow reduction for trailing aircraft (NASA, 2002)

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## Extended Formations



- ~15-40 span separation
- A safer approach to formation flight
- Can be implemented with today's aircrafts without modification
- Up to 10% fuel flow reduction for transport aircraft\*



\*Pahle, Joe, "A preliminary Investigation of Formation Flight for Drag Reduction on the C-17 aircraft"

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## Extended Formations



- Provides a safer approach to formation flying, yet retains much of the fuel savings seen in close formation flight

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## Extended Formations

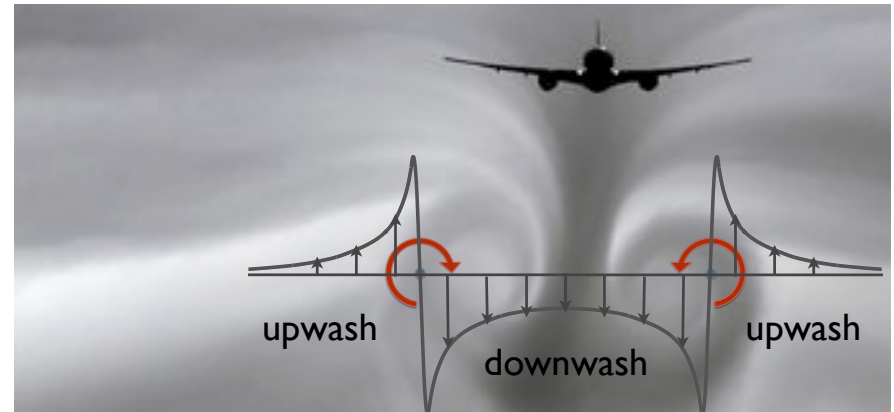


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## Extended Formations

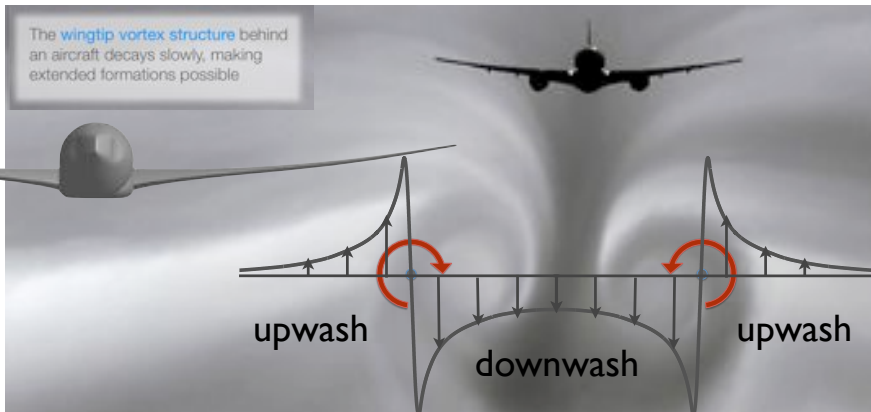


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## Extended Formations



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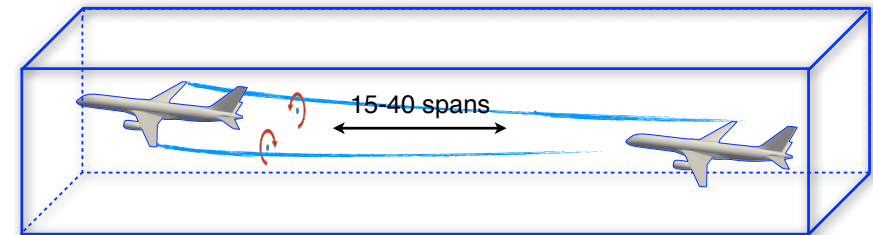
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## Modeling



- In close formation, the trailing aircraft can influence the lead
- At 15-40 spans separation, this effect becomes negligible
- Extended formations decouple lead and follower aircraft



Lead Aircraft

Trail Aircraft

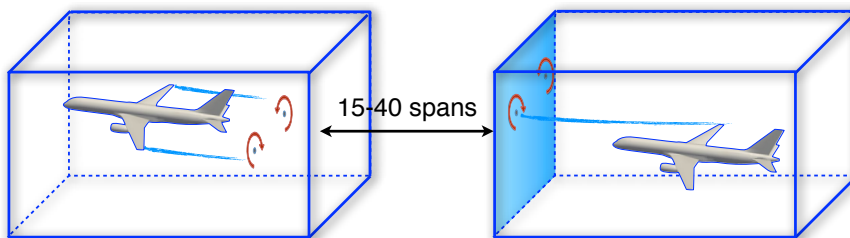
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## Modeling



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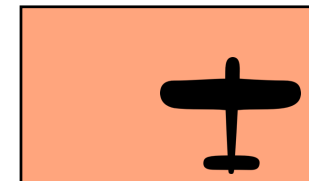
Lead Aircraft

Trail Aircraft

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## Modeling Approach



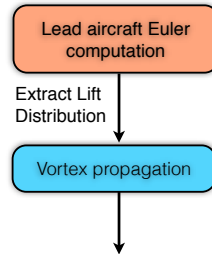
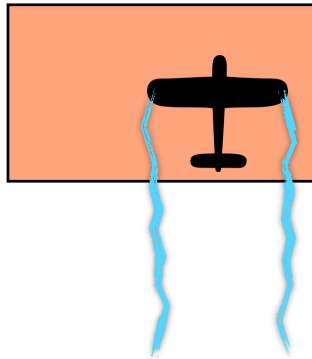
Lead aircraft Euler  
computation

Extract Lift  
Distribution

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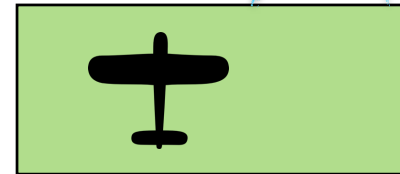
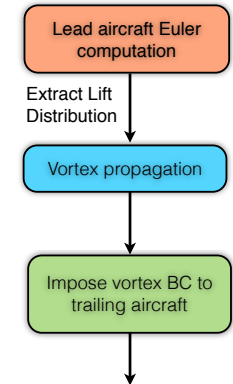
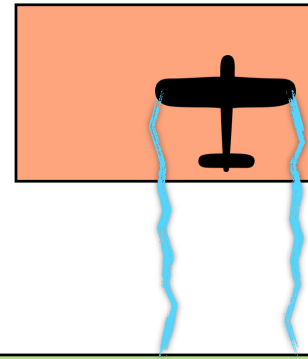
12

## Modeling Approach



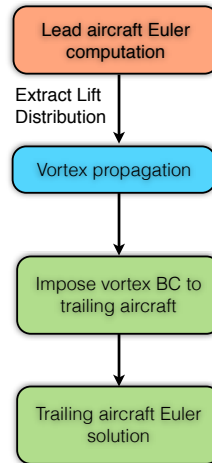
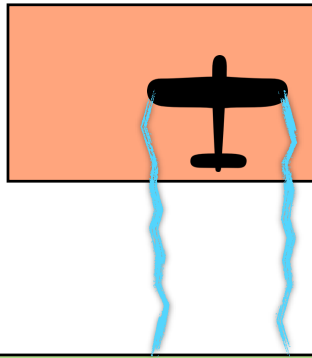
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## Modeling Approach



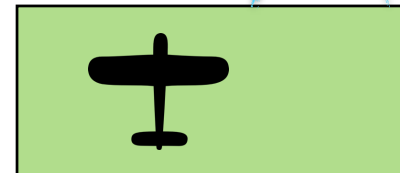
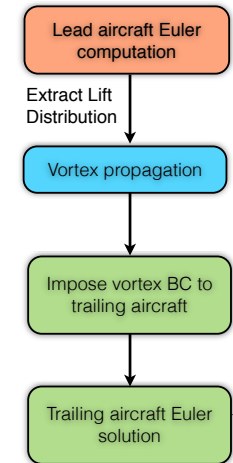
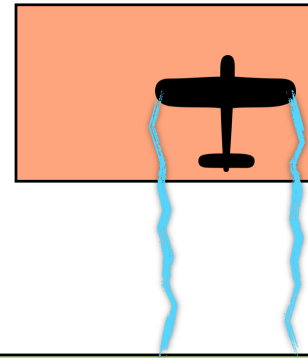
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## Modeling Approach



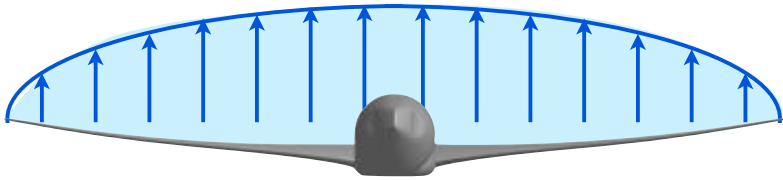
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## Modeling Approach

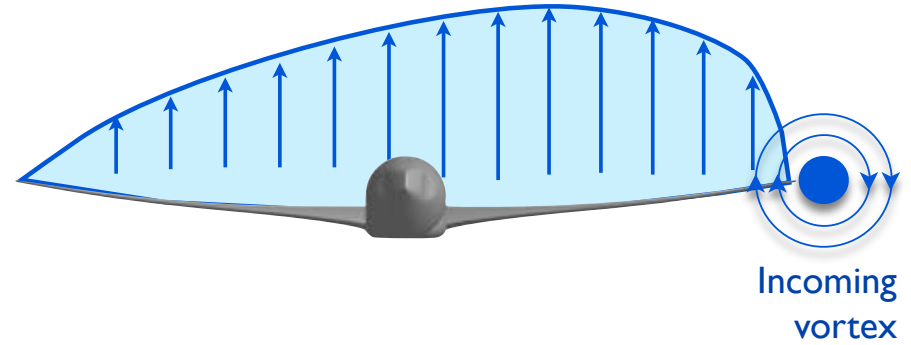


16

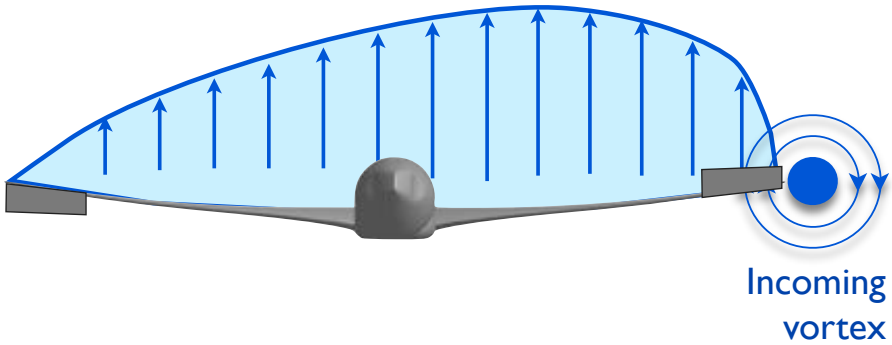
## Out-of-Formation



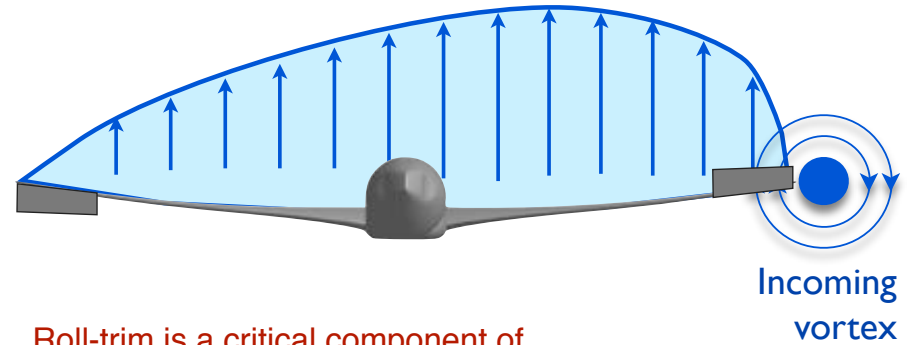
## In-Formation



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## In-Formation



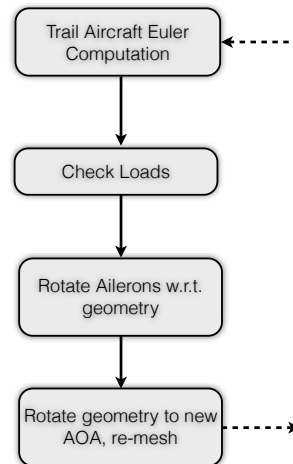
Roll-trim is a critical component of  
formation flying

## Roll-Trim Strategy



### Algorithm for trim:

- (1) Compute trail A/C flow solution
- (2) Check Lift & Roll tolerance
- (3) Deflect ailerons if necessary (roll)
- (4) Adjust AOA if necessary (lift)

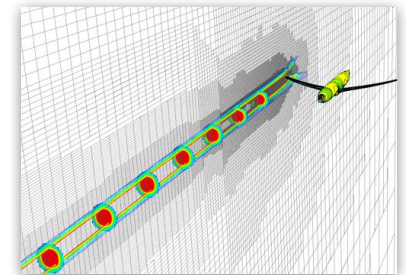


## Flow Analysis: Cart3D



Requirements: automatic control surface deflections, geometry re-meshing, and high-fidelity CFD solutions

- Inviscid analysis package, 3D compressible Euler equations
- Unstructured Cartesian cells with cut-cells at wall
- Adjoint-Based Mesh Adaptation
- Highly automated for parameter sweeps, geometry manipulation, and re-meshing



## Flow Analysis: Objective Functional



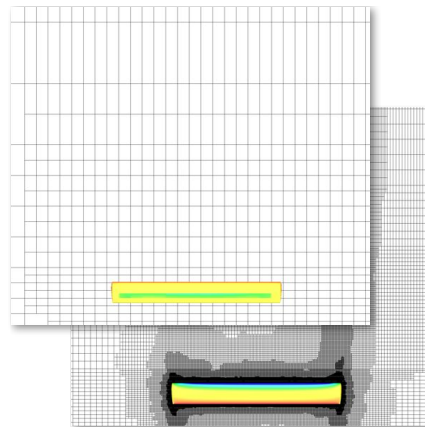
- Formation flight aims to improve induced drag at fixed lift...

$$C_{Di} = \frac{C_L^2}{\pi AR e}$$

- Span efficiency factor,  $e$ , is a natural choice

$$e = \frac{C_L^2}{\pi AR C_{Di}}$$

Initial Mesh (100k cells)



## Flow Analysis: Objective Functional



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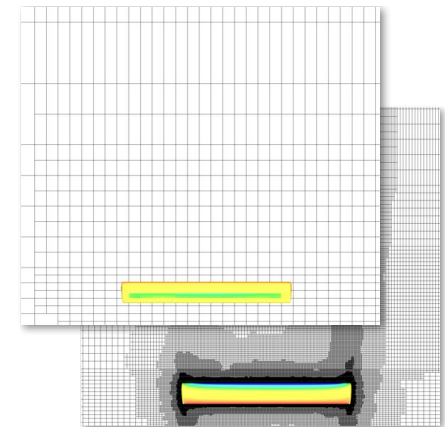
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$C_L \sim 0.5$   
 $C_D \sim 0.008$

Initial Mesh (100k cells)



## Flow Analysis: Objective Functional



- Formation flight aims to improve induced drag at fixed lift...

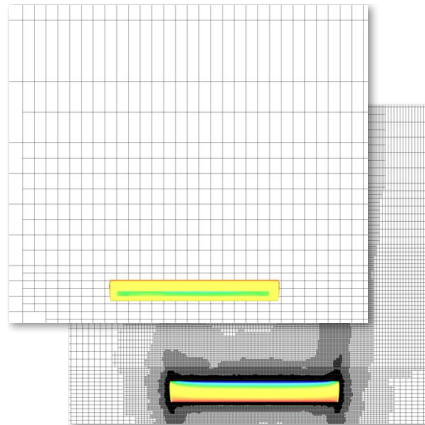
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$$e = \frac{C_L^2}{\pi AR C_{Di}} \quad C_L \sim 0.5 \quad C_D \sim 0.008$$

Expensive to converge due to drag sensitivity

Initial Mesh (100k cells)



## Flow Analysis: Objective Functional



- Formation flight aims to improve induced drag at fixed lift...

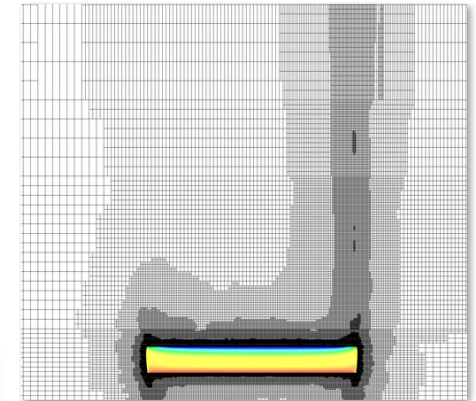
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Expensive to converge due to drag sensitivity

Final mesh (20 mil. cells)



## Results Outline



- Mesh convergence study
- Incompressible Effects
  - roll-trim
  - Vortex position sensitivity
- Compressible Effects
  - roll-trim



## Formation flight metric



$$\text{drag fraction} = \frac{\sum D_{\text{in formation}}}{\sum D_{\text{out formation}}}$$

- Provides a measure for overall drag savings of the formation
- Focus on 2-aircraft echelon formations...

$$\text{drag fraction} = \frac{D_{\text{lead}} + D_{\text{trail}}}{2D_{\text{lead}}}$$

Ex.: a drag fraction of 0.9 represents a 10% drag savings in formation flight



## Results: Vortex in empty domain

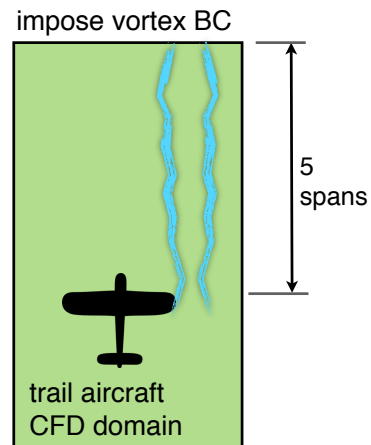


### Flow conditions

- Mach = 0.5
- CL (lead A/C) = 0.55
- Objective Function: Integrated pressure at 5 spans from inflow

### Goal

- Verify mesh convergence of vortex in absence of geometry



## Results: Vortex in empty domain

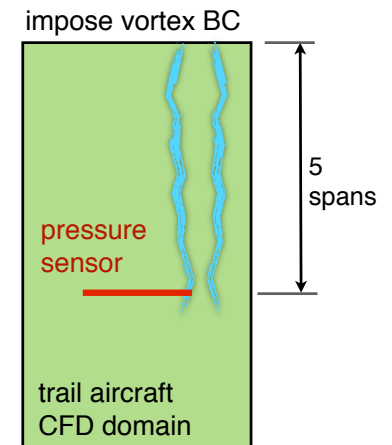


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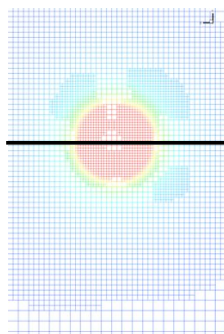
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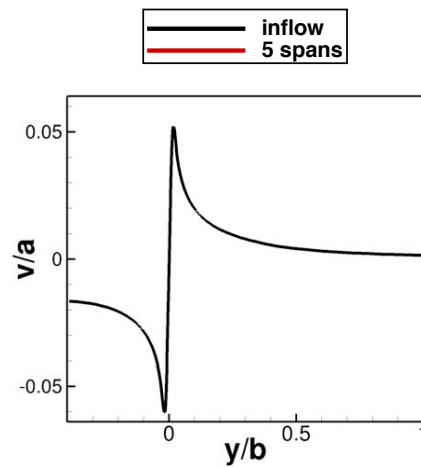
- Verify mesh convergence of vortex in absence of geometry



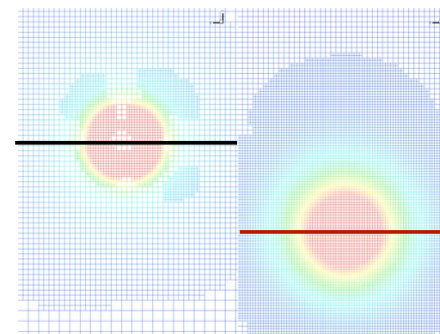
## Results: Vortex in empty domain



Inflow

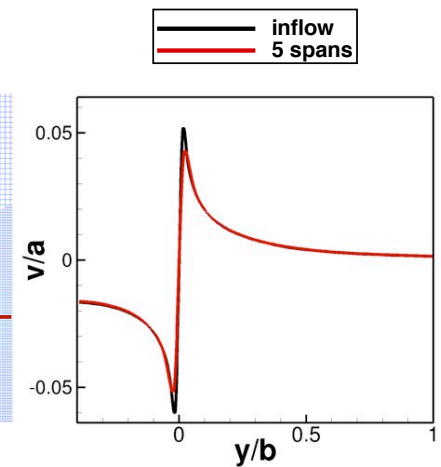


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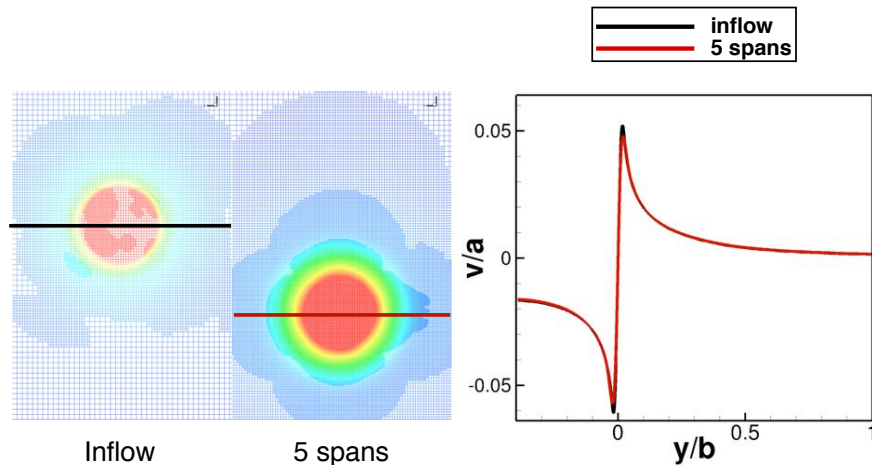
Inflow

5 spans





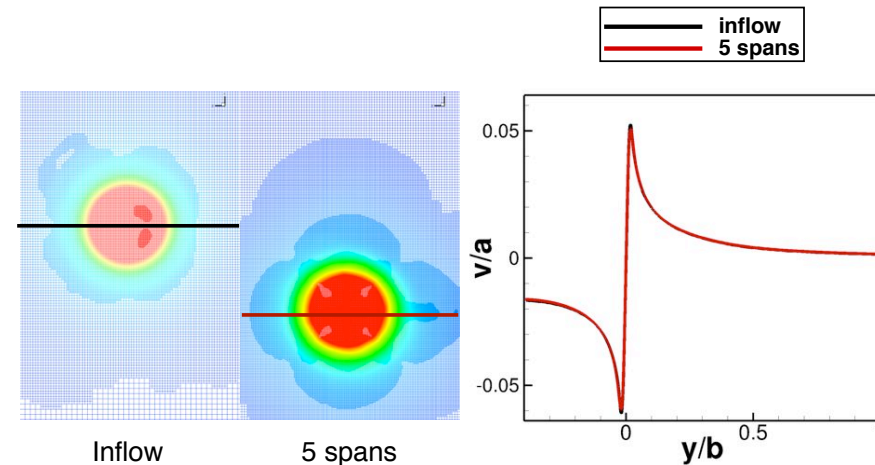
## Results: Vortex in empty domain



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## Results: Vortex in empty domain



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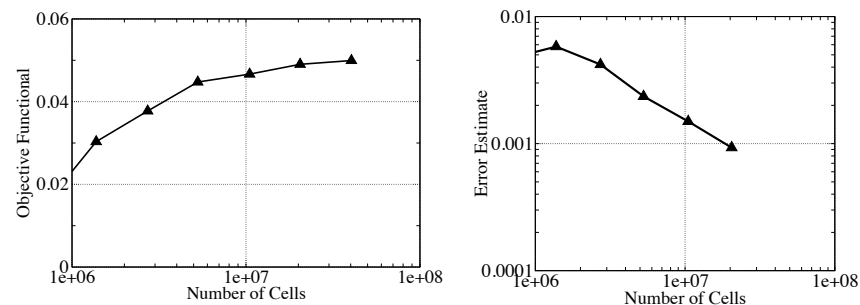
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## Results: Vortex in empty domain



Mach = 0.5

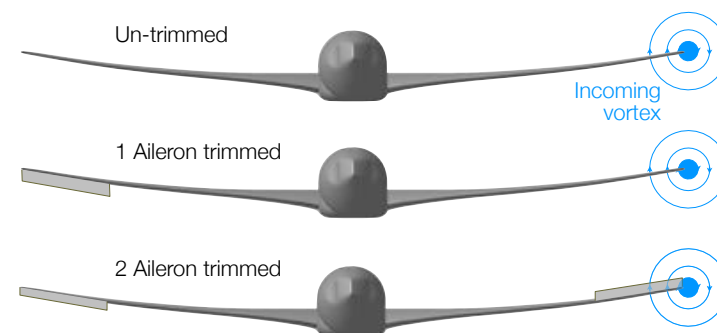
- Objective functional: integrated pressure 5 spans downstream



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## Results: Trimming Configurations



- un-trimmed (baseline) configuration contains no ailerons
- 1-aileron deflected; increases lift on out-of-vortex wing
- 2-aileron deflected; trims in conventional manner

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## Results: Simple Wing

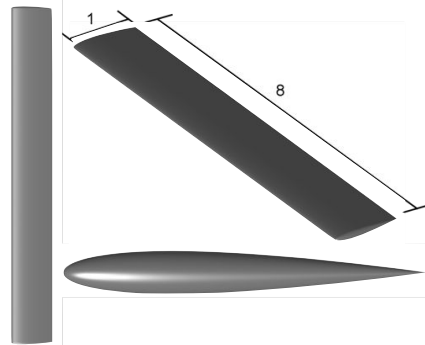


### Geometry

- Sub-sonic straight wing w/ NACA 0012 sections

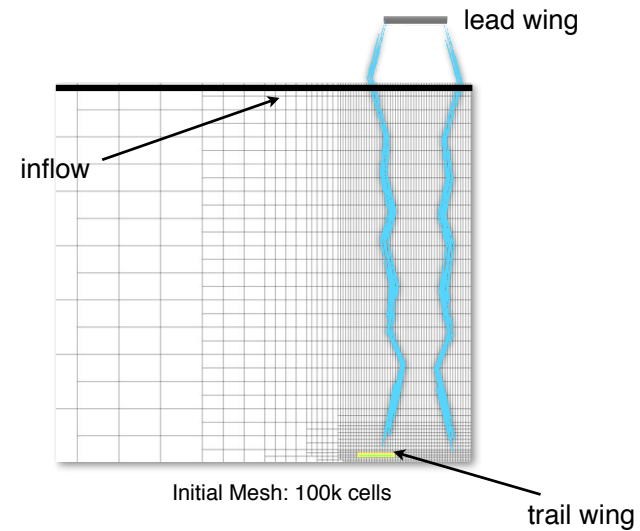
### Goals

- Quantify/Verify incompressible formation flight drag savings
- Roll-trim effects
- Determine trail A/C position sensitivity

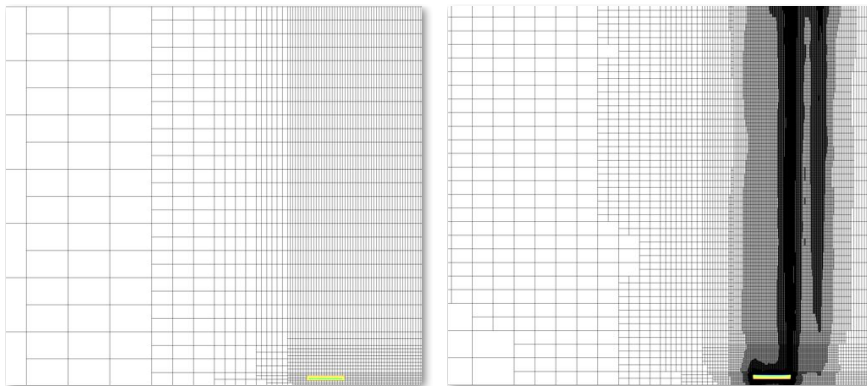


Geometry	$C_L$	$M_\infty$	AR	$S_{ref}(ft^2)$
NACA 0012 Wing	0.55	0.5	8	8

## Results: Simple Wing



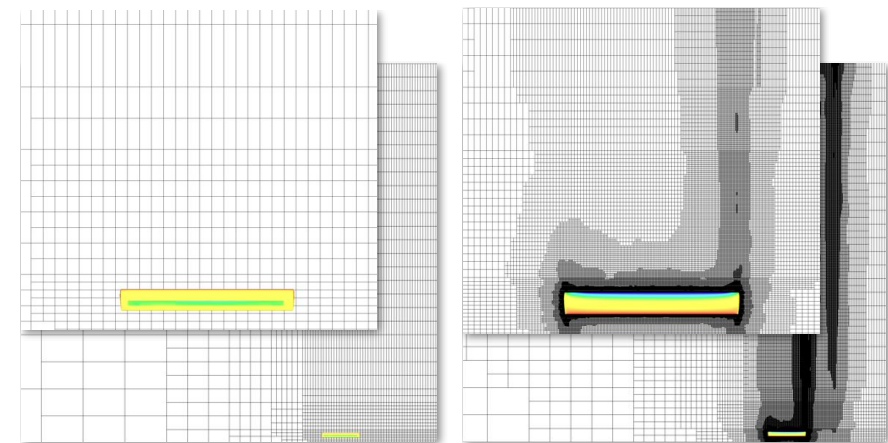
## Results: Simple Wing



Initial Mesh: 100k cells

Final Mesh: 20 Mil. cells

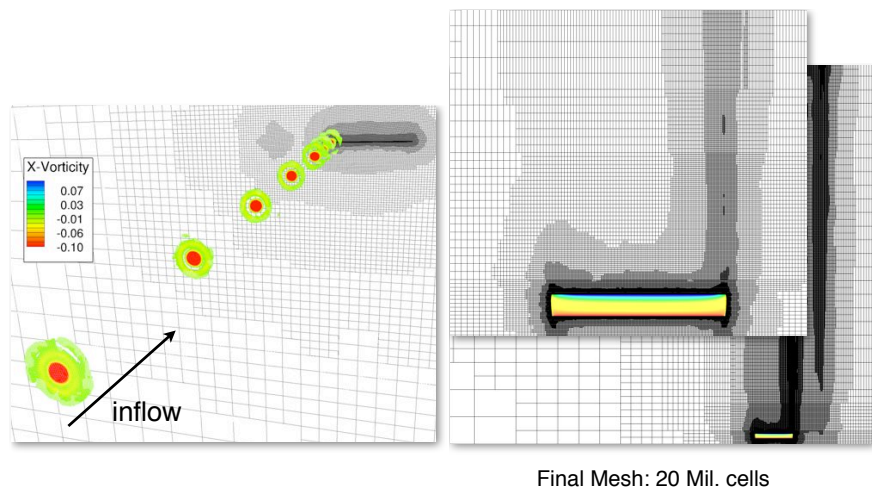
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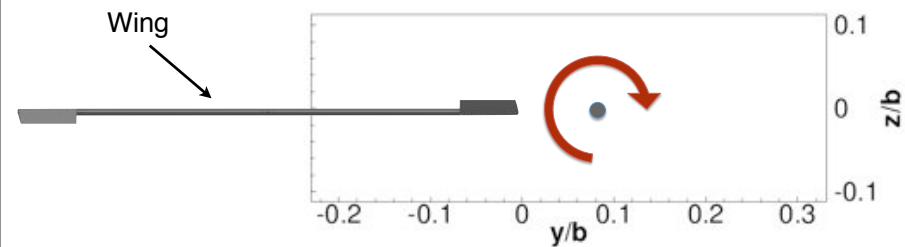
## Results: Simple Wing



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## Results: Vortex Position Sensitivity

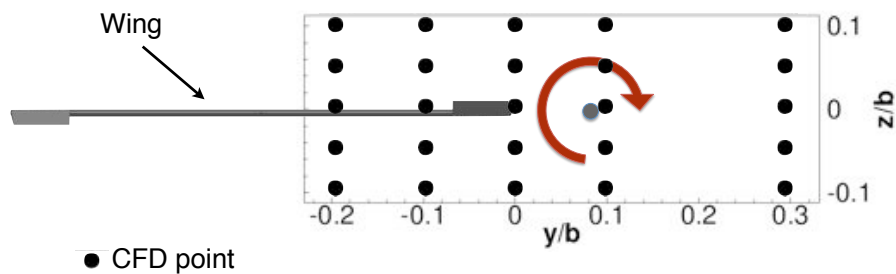


\*View behind wing facing upstream

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## Results: Vortex Position Sensitivity

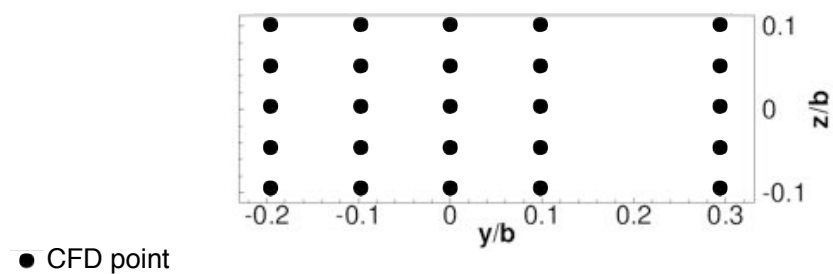


\*View behind wing facing upstream

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## Results: Vortex Position Sensitivity

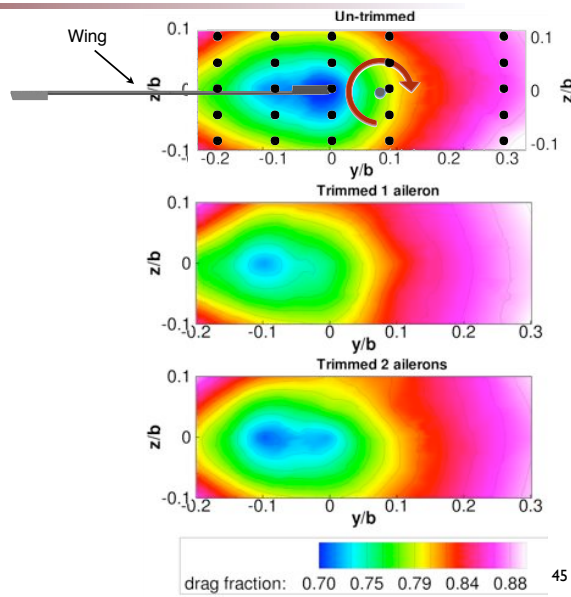


\*View behind wing facing upstream

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## Results: Vortex Position Sensitivity



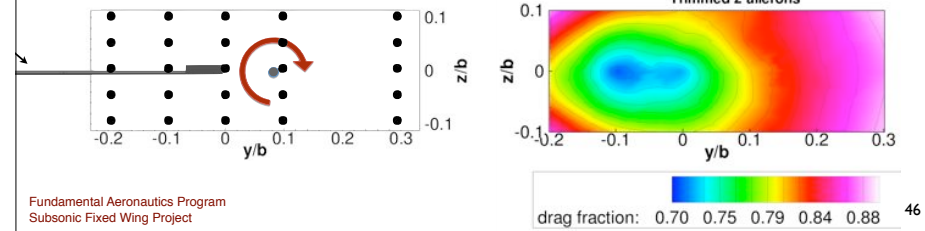
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## Results: Vortex Position Sensitivity



- Optimal vortex location migrates inboard w/ trim
- 2-aileron outperforms 1-aileron trim
- 3-5% decrease in drag fraction for 2-aileron



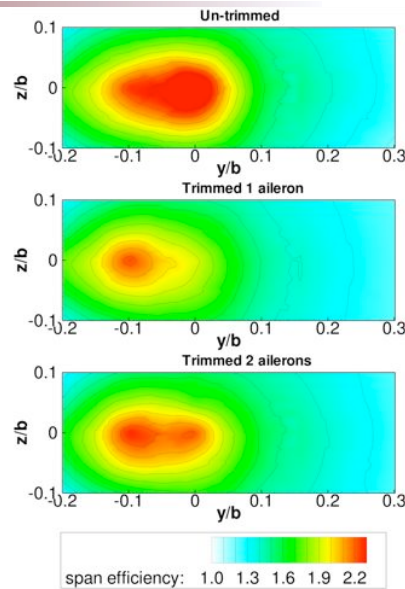
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## Results: Vortex Position Sensitivity



- un-trimmed, optimal span efficiency ~2.2 @ wingtip
- Optimal vortex location migrates inboard w/ trim
- 2-aileron trimmed outperforms 1-aileron



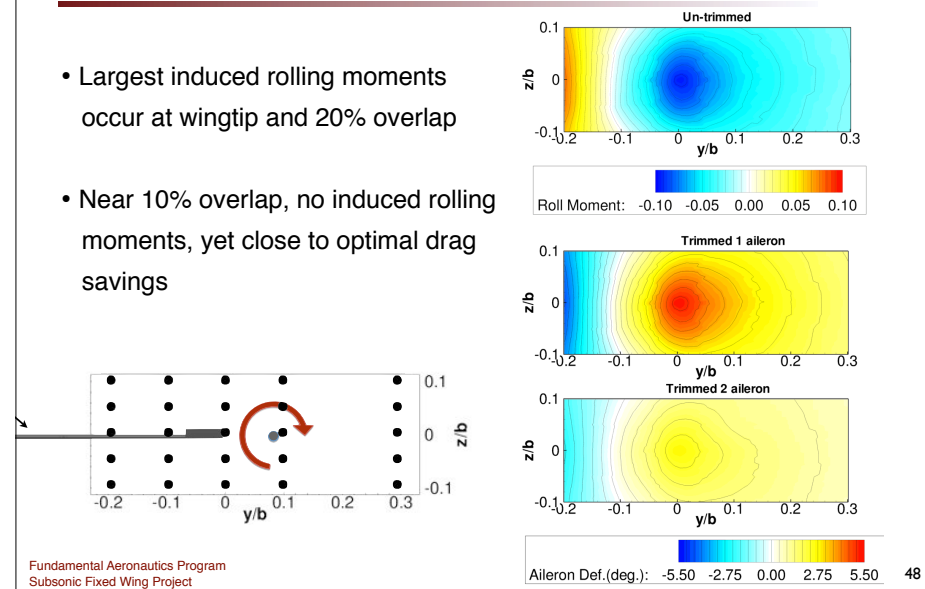
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## Results: Vortex Position Sensitivity



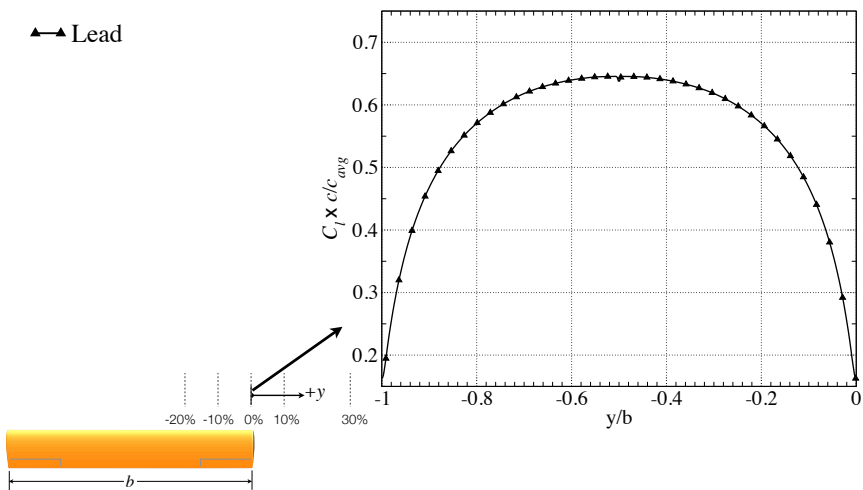
- Largest induced rolling moments occur at wingtip and 20% overlap
- Near 10% overlap, no induced rolling moments, yet close to optimal drag savings



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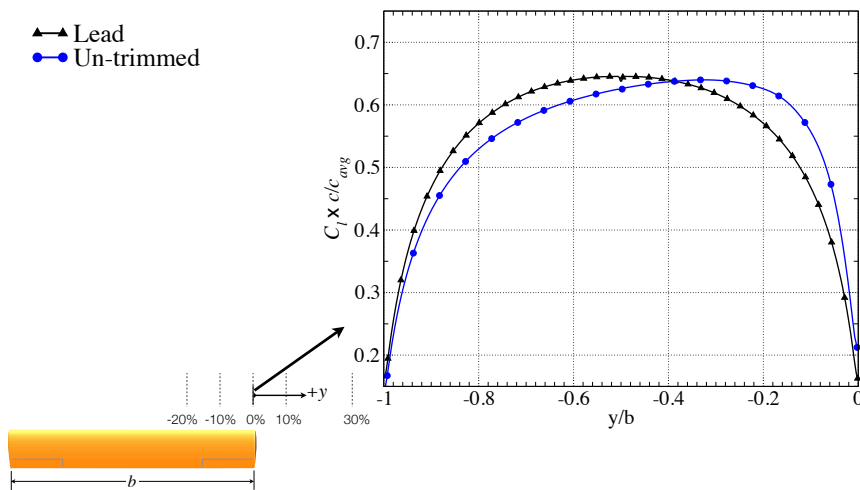
## Results: Vortex Position Sensitivity



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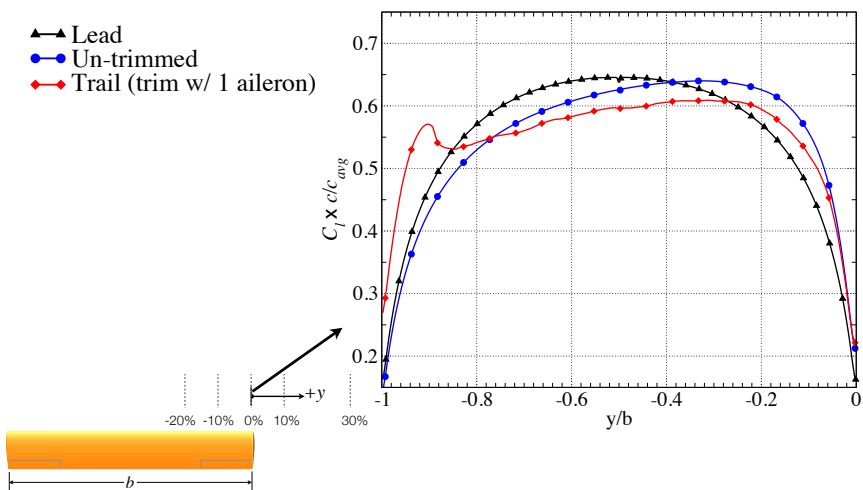
## Results: Vortex Position Sensitivity



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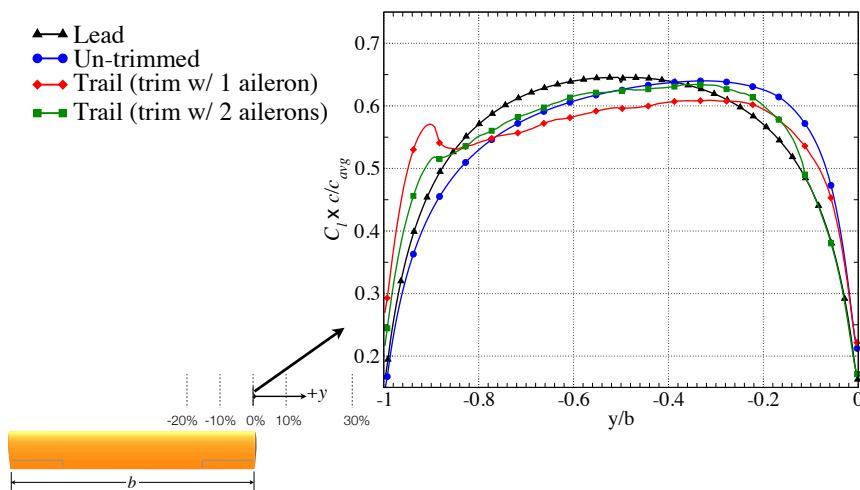
## Results: Vortex Position Sensitivity



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## Results: Vortex Position Sensitivity

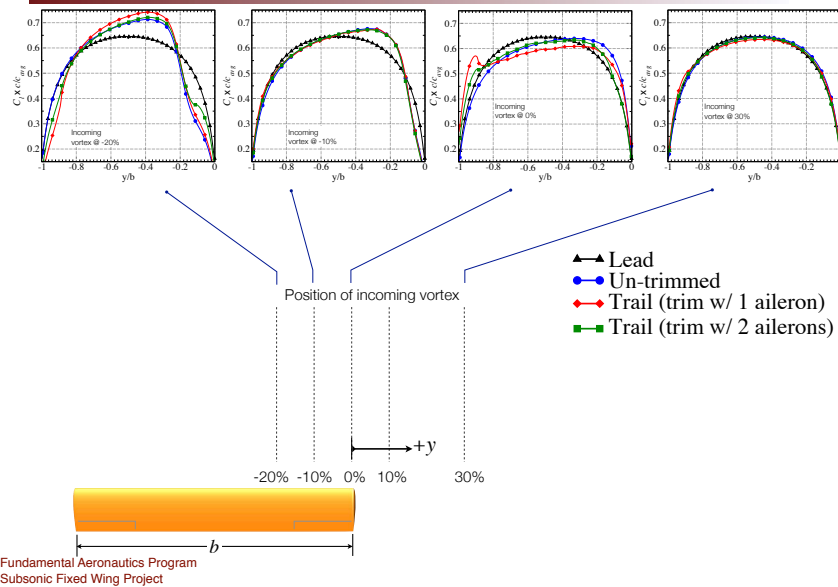


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## Results: Vortex Position Sensitivity



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## Results: Common Research Model

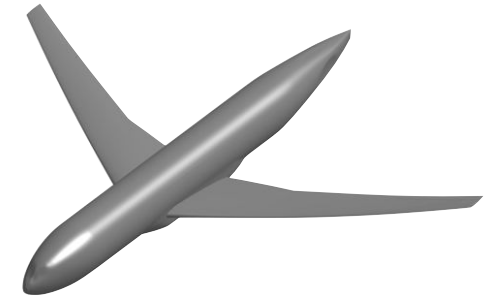


### Geometry

- Modified CRM from 4th AIAA Drag Prediction Workshop\*

### Goals

- Quantify compressible formation flight drag savings
- Determine roll-trim effects on more realistic wing/body geometry



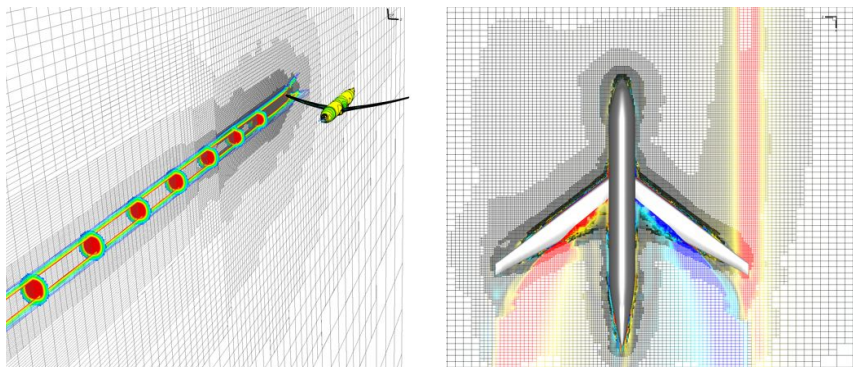
Geometry	$C_L$	$M_\infty$	AR	$S_{ref}(ft^2)$
CRM	0.5	0.83	9	4130

\*Vassberg, J. C., et al. Development of a Common Research Model for Applied CFD Validation Studies, AIAA Applied Aerodynamics Conference, AIAA 2008-6919, August 2008.

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## Results: CRM

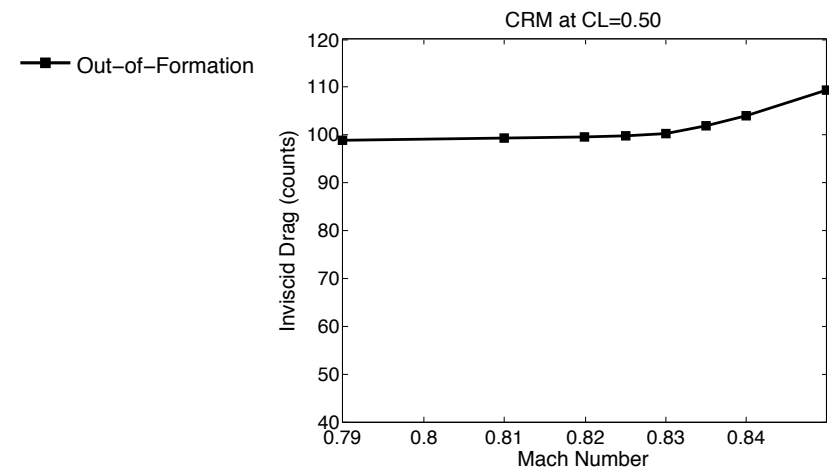


Final Mesh: 40 Mil. cells

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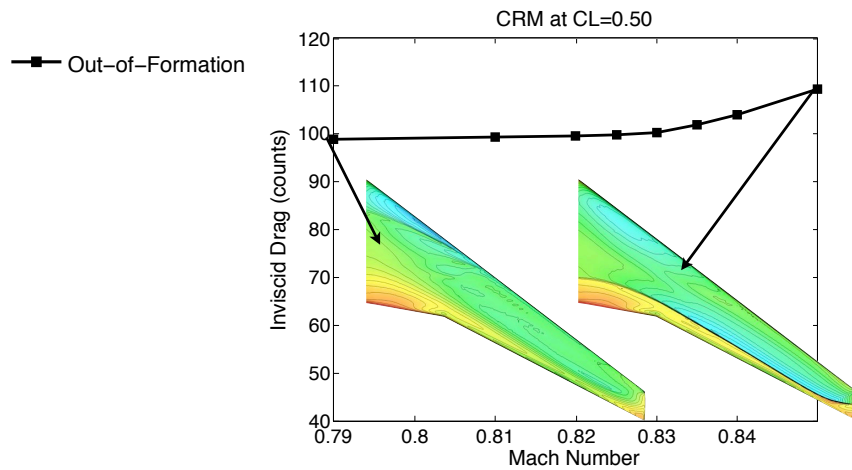
## Results: CRM



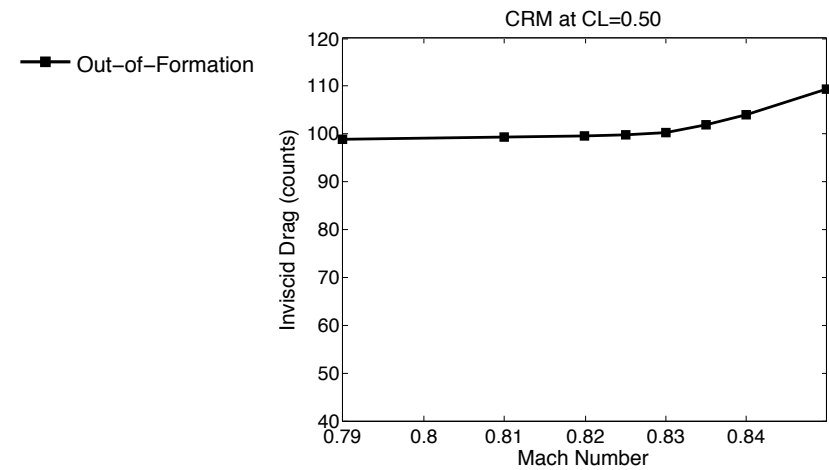
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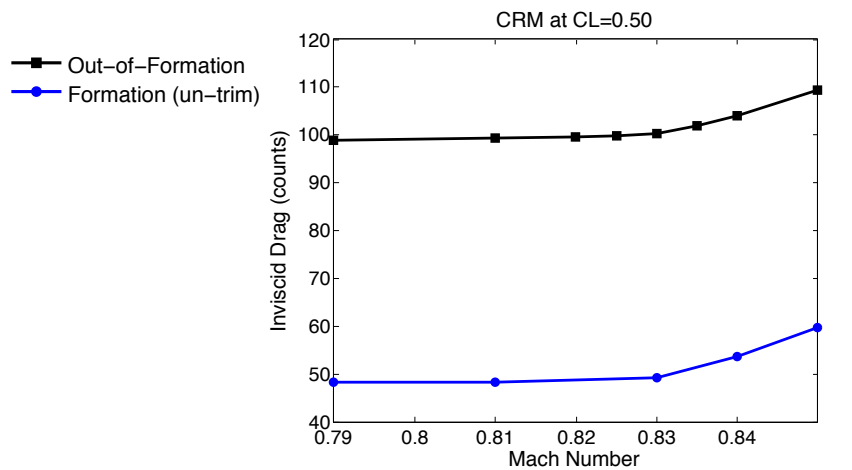
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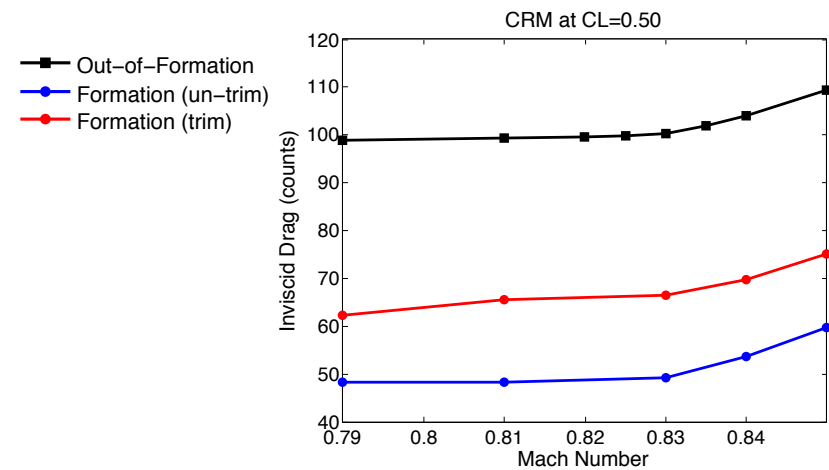
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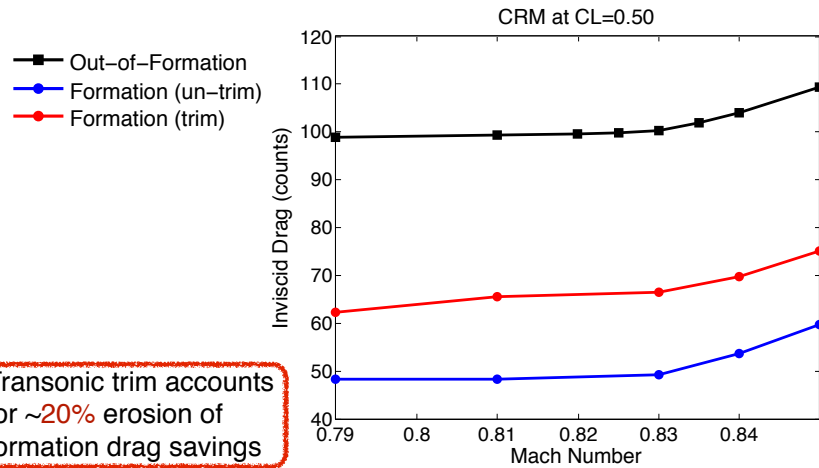


## Results: CRM





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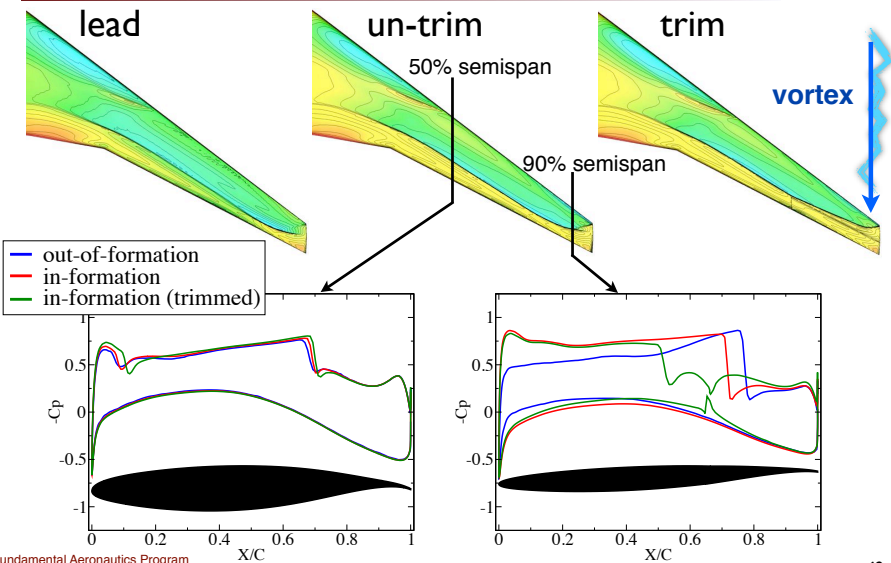


Transonic trim accounts for ~20% erosion of formation drag savings

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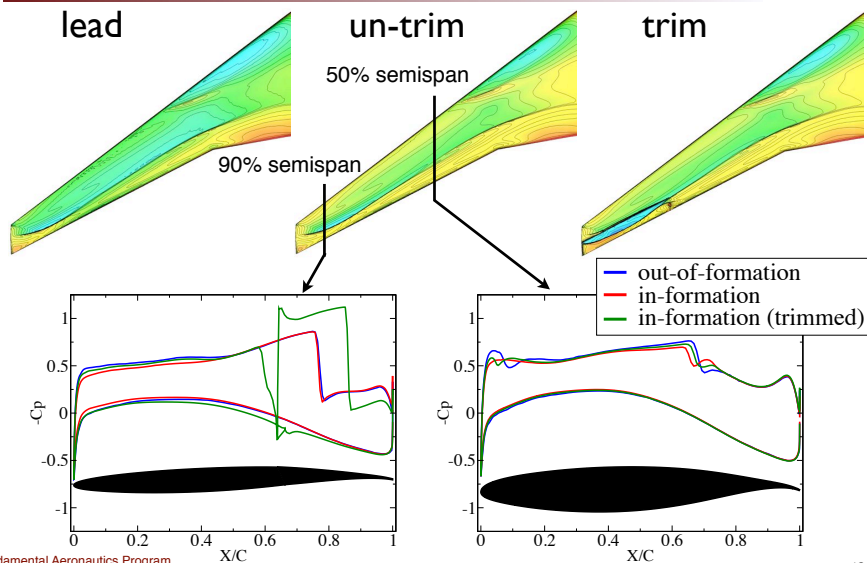
## CRM, Mach = 0.83



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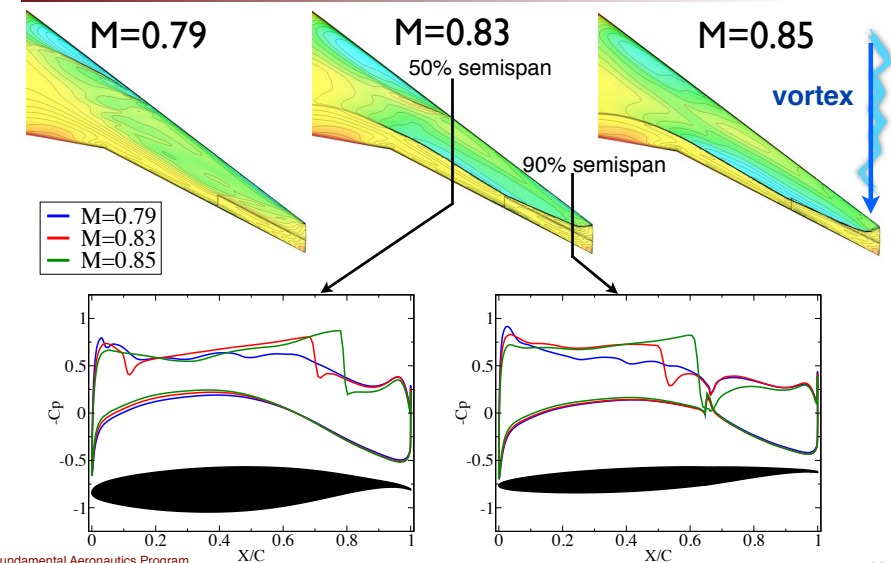
## CRM, Mach = 0.83



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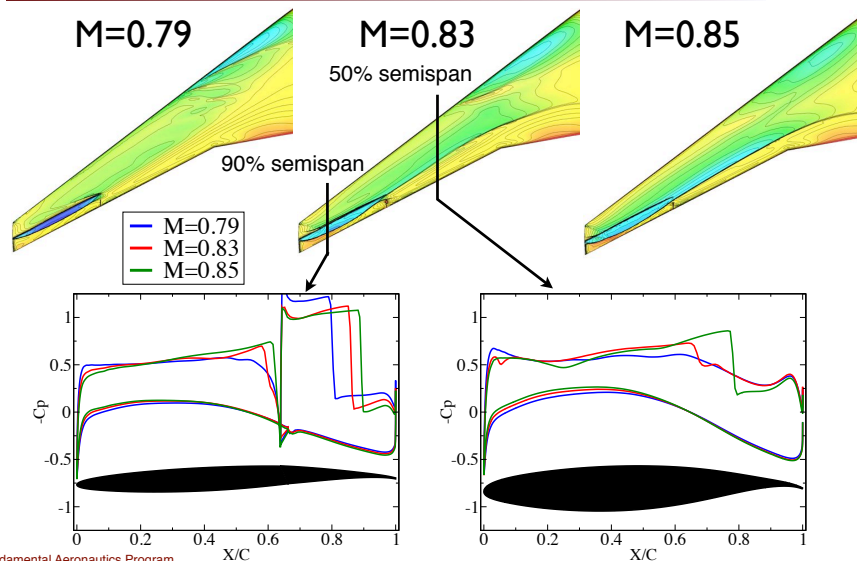
## CRM, In-Formation, trimmed



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## CRM, In-Formation, trimmed



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## Summary



- Performed relevant verification for vortex boundary condition
- Developed methodology for evaluating formation flight benefits for 2-aircraft echelon formations
- Developed quantitative benefit maps for trail aircraft positioning
- Evaluated erosion of formation flight benefits as a result of trim and compressibility

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## Open Issues



- Complete benefits map for summer conference
- Extend analysis to > 2 aircraft formations
- Effects of heterogeneous aircrafts in formation
- Deliver analytic drag model for formation flight including trim/compressibility for use in NAS models

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## Wake Propagation Model



### Augmented Betz Method\*

- Far-field conservation method
- Experimental core-size data
- LES vortex decay rates

### Assumptions

- Viscous effects neglected during rollup
- All vorticity from lead is axis-symmetrically rolled-up into 2 vortices

\*Ning, Andrew, Aerodynamic Performance of Extended Formation Flight, Journal of Aircraft, Vol. 48, No. 3, May-June 2011

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### Governing Equations:

#### continuity:

$$\frac{\partial u_y}{\partial y} + \frac{\partial u_z}{\partial z} = 0$$

#### vorticity:

$$\frac{\partial \zeta}{\partial t} + u_y \frac{\partial \zeta}{\partial y} + u_z \frac{\partial \zeta}{\partial z} = \nu \left( \frac{\partial^2 \zeta}{\partial y^2} + \frac{\partial^2 \zeta}{\partial z^2} \right)$$

$$\left( \text{where } \zeta = \frac{\partial u_z}{\partial y} - \frac{\partial u_y}{\partial z} \right)$$

### Time Invariants:

$$\Gamma_0 = \int \zeta dA$$

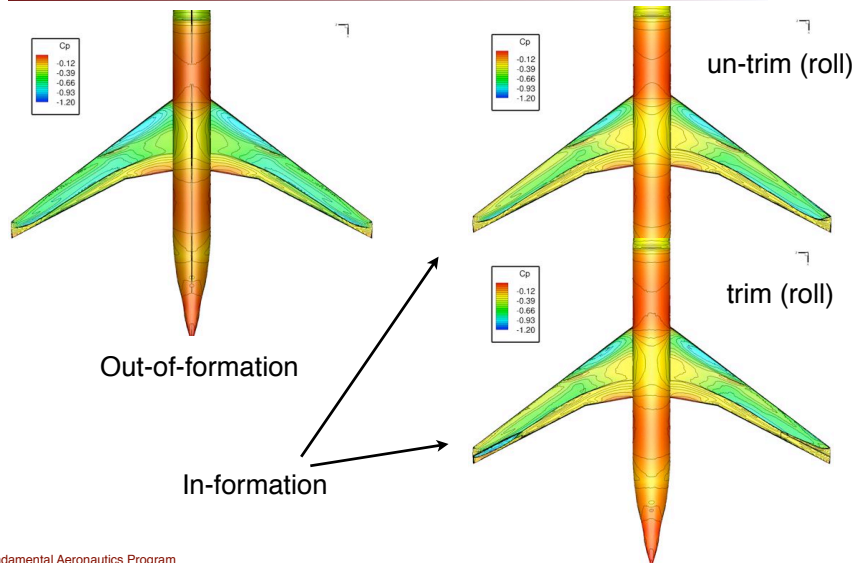
$$\Gamma_y = \int y \zeta dA$$

$$\Gamma_z = \int z \zeta dA$$

$$\Gamma_r = \int (y^2 + z^2) \zeta dA$$

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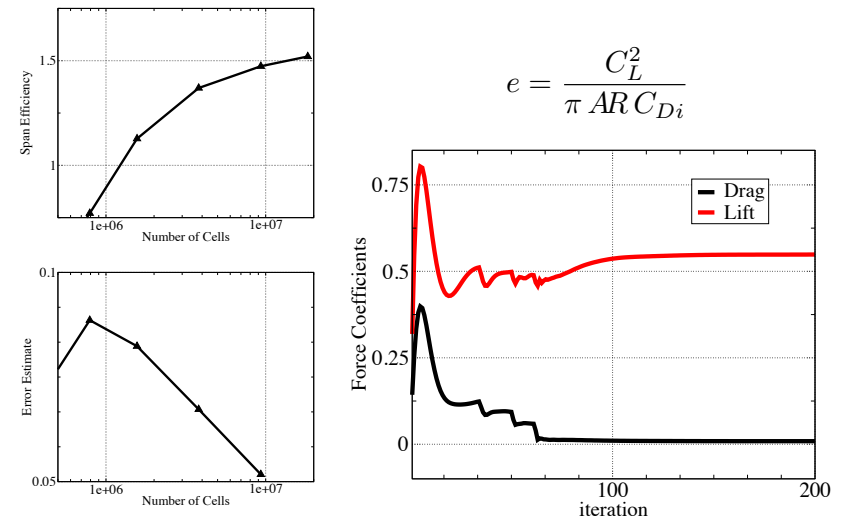
## Results: CRM at M=0.83



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## Results: Simple Wing



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